

Aim: How do we multiply and divide more complicated radicals?

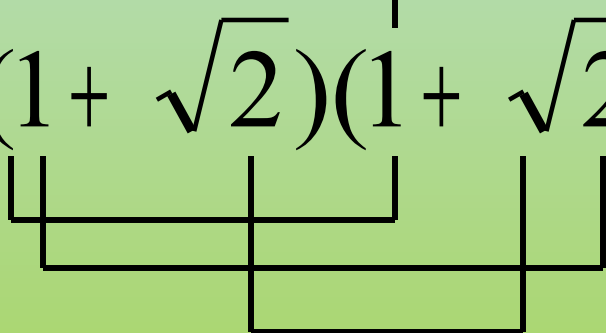
Do Now: 1. Multiply: $(1 + x)(1 + x)$

2. Multiply: $(1 + \sqrt{2})(1 + \sqrt{2})$

3. Divide: $\frac{15x^3 + 5x^2}{5x}$

4. Divide: $\frac{15\sqrt{8} - 5\sqrt{6}}{5\sqrt{2}}$

To multiply binomials involved radicals, we can treat the radical as a variable and use the **FOIL** method.

$$(1 + \sqrt{2})(1 + \sqrt{2}) = 1^1 + \sqrt{2} + \sqrt{2} + \sqrt{2}^2$$

$$= 1 + 2\sqrt{2} + 2 = 3 + 2\sqrt{2}$$

$$(3 + \sqrt{6x})(1 + \sqrt{2x}) = 3 + 3\sqrt{2x} + \sqrt{6x} + \sqrt{12x^2}$$
$$= 3 + 3\sqrt{2x} + \sqrt{6x} + \sqrt{4 \cdot 3x^2}$$
$$= 3 + 3\sqrt{2x} + \sqrt{6x} + 2x\sqrt{3}$$

To divide $\frac{15\sqrt{8} - 5\sqrt{6}}{5\sqrt{2}}$

we can separate the fraction into two fractions as

$$\frac{15\sqrt{8}}{5\sqrt{2}} - \frac{5\sqrt{6}}{5\sqrt{2}} = 3\sqrt{\frac{8}{2}} - \sqrt{\frac{6}{2}} = 3\sqrt{4} - \sqrt{3} = 6 - \sqrt{3}$$

Simplify: $\frac{12\sqrt{10a^2b} + 8\sqrt{15ab^2}}{4\sqrt{5ab}} = \frac{12\sqrt{10a^2b}}{4\sqrt{5ab}} + \frac{8\sqrt{15ab^2}}{4\sqrt{5ab}}$

$$= 3\sqrt{\frac{10a^2b}{5ab}} + 2\sqrt{\frac{15ab^2}{5ab}} = 3\sqrt{2a} + 2\sqrt{3b}$$

Express the product in simplest form

$$(3 - \sqrt{6})(5 + \sqrt{6})$$

$$9 - 2\sqrt{6}$$

$$(9 + \sqrt{2x})(1 + \sqrt{2x})$$

$$2x + 9 + 10\sqrt{2x}$$

$$(7 + \sqrt{5a})(7 - \sqrt{5a})$$

$$49 - 5a$$

$$\frac{3\sqrt{10} - 9\sqrt{50}}{3\sqrt{5}}$$

$$\sqrt{2} - 3\sqrt{10}$$

$$\frac{\sqrt[3]{27x^3} + \sqrt[3]{36x^5}}{\sqrt[3]{3x^3}}$$

$$\sqrt[3]{9} + \sqrt[3]{12x^2}$$