

## Worksheet #15

## Answers

1)  $\sqrt{2x} = 10$

$2x = 100$

$x = 50$

ch:  $\sqrt{2(50)} - 10 = 0$

$\sqrt{100} - 10 = 0$

$0 = 0 \checkmark$

2)  $\sqrt{5-x} = 3$

$5-x = 9$

$-x = 4$

$x = -4$

ch:  $\sqrt{5-(-4)} - 3 = 0$

$\sqrt{9} - 3 = 0$

$0 = 0 \checkmark$

3)  $\sqrt[3]{2x+5} = -3$

$2x+5 = -27$

$2x = -32$

$x = -16$

ch:  $\sqrt[3]{2(-16)+5} + 3 = 0$

$\sqrt[3]{-27} + 3 = 0$

$-3 + 3 = 0$

$0 = 0 \checkmark$

4)  $\sqrt[3]{3x+1} = 5$

$3x+1 = 125$

$3x = 124$

$x = 124/3$

ch:  $\sqrt[3]{3(124/3)+1} - 5 = 0$

$\sqrt[3]{125} - 5 = 0$

$0 = 0 \checkmark$

5)  $x+5 = x-5$

$0 = 0$

$x = \{ \}$

6)  $\sqrt{x-20} = 10 - \sqrt{x}$

$x-20 = 100 - 20\sqrt{x} + x$

$-20 = 100 - 20\sqrt{x}$

$-120 = -20\sqrt{x}$

$6 = \sqrt{x}$

$36 = x$

ch:  $\sqrt{(36)} + \sqrt{(36)} - 20 = 10$

$6 + 4 = 10$

$10 = 10$

7)  $3x+2 = 7 \quad | \quad 3x+2 = -7$

$3x = 5$

$3x = -9$

$x = 5/3$

$x = -3$

ch:  $|3(5/3)+2| = 7 \quad |3(-3)+2| = -7$

$|5+2| = 7$

$|-9+2| = -7$

$7 = 7$

$7 \neq -7$

$x = \{5/3\}$

8)  $x = x^2 + x - 3 \quad | \quad -x = x^2 + x - 3$

$0 = x^2 - 3$

$0 = x^2 + 2x - 3$

$3 = x^2$

$(x+3)(x-1) = 0$

$x = \pm \sqrt{3}$

$x = \{-3, 1\}$

ch:  $|\sqrt{3}| = 3 + \sqrt{3} - 3$

$\sqrt{3} = \sqrt{3}$

$|- \sqrt{3}| = 3 - \sqrt{3} - 3$

$\sqrt{3} \neq -\sqrt{3}$

$|-3| = 9 - 3 - 3 \quad |1| = 1 + 1 - 3$

$3 = 3$

$1 \neq -1$

$x = \{\sqrt{3}, 3\}$

9) decreases:  $-\infty < x < -1$

increases:  $-1 < x \leq 4$

10) increases:  $-\infty < x \leq 1$