

From Houghton-Mifflin Precalculus

3rd Edition

p701:

14) $(x + 5) + (y - 1)^2 = 0 \rightarrow (y - 1)^2 = -1(x + 5)$ horizontal

vertex: $(-5, 1)$, $4p = -1$, $p = -1/4$

focus: $(h + p, k) = (-5.25, 1)$, directrix: $x = h - p$, $x = -4.75$

15) $(x + \frac{3}{2})^2 = 4(y - 2)$ vertical

vertex: $(-\frac{3}{2}, 2)$, $4p = 4$, $p = 1$

focus: $(h, k + p) = (-\frac{3}{2}, 3)$, directrix: $y = k - p$, $y = 1$

17) $y = \frac{1}{4}(x^2 - 2x + 5) \rightarrow 4y = x^2 - 2x + 5 \rightarrow 4y = (x^2 - 2x + 1) + 5 - 1$

$\rightarrow 4y - 4 = (x - 1)^2 \rightarrow (x - 1)^2 = 4(y - 1)$ vertical

vertex = $(1, 1)$, $4p = 4$, $p = 1$

focus: $(h, k + p) = (1, 2)$, directrix: $y = k - p$, $y = 0$

18) $x = \frac{1}{4}(y^2 + 2y + 33) \rightarrow 4x - 33 = y^2 + 2y \rightarrow 4x - 33 + 1 = y^2 + 2y + 1$

$\rightarrow 4(x - 8) = (y + 1)^2$ horizontal

vertex: $(8, -1)$, $4p = 4$, $p = 1$

focus: $(h + p, k) = (9, -1)$, directrix: $x = h - p$, $x = 7$

19) $y^2 + 6y + 8x + 25 = 0 \rightarrow y^2 + 6y = -8x - 25 \rightarrow$

$y^2 + 6y + 9 = -8x - 25 + 9 \rightarrow (y + 3)^2 = -8(x + 2)$ horizontal

vertex: $(-2, -3)$, $4p = -8$, $p = -2$

focus: $(h + p, k) = (-4, -3)$, directrix: $x = h - p$, $x = 0$

20) $y^2 - 4y - 4x = 0 \rightarrow y^2 - 4y = 4x \rightarrow y^2 - 4y + 4 = 4x + 4$

$\rightarrow (y - 2)^2 = 4(x + 1)$ horizontal

vertex: $(-1, 2)$, $4p = 4$, $p = 1$

focus: $(h + p, k) = (0, 2)$, directrix: $x = h - p$, $x = -2$

p382:

72) $(\cot x + \csc x)(\cot x - \csc x) = \cot^2 x - \csc^2 x = -1$

73) $(\sec x + 1)(\sec x - 1) = \sec^2 x - 1 = \tan^2 x$